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A minimal robophysical model of quadriflagellate self-propulsion

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Abstract

Locomotion at the microscale is remarkably sophisticated. Microorganisms have evolved diverse strategies to move within highly viscous environments, using deformable, propulsion-generating appendages such as cilia and flagella to drive helical or undulatory motion. In single-celled algae, these appendages can be arranged in different ways around an approximately 10 \(\mu\)m long cell body, and coordinated in distinct temporal patterns. Inspired by the observation that some quadriflagellates (bearing four flagella) have an outwardly similar morphology and flagellar beat pattern, yet swim at different speeds, this study seeks to determine whether variations in swimming performance could arise solely from differences in swimming gait. Robotics approaches are particularly suited to such investigations, where the phase relationships between appendages can be readily manipulated. Here, we developed autonomous, algae-inspired robophysical models that can self-propel in a viscous fluid. These macroscopic robots (length and width = 8.5 cm, height = 2 cm) have four independently actuated ‘flagella’ (length = 13 cm) that oscillate under low-Reynolds number conditions (Re \(\sim\) \(\mathcal{O}(10^{-1})\)). We tested the swimming performance of these robot models with appendages arranged two distinct configurations, and coordinated in three distinct gaits. The gaits, namely the pronk, the trot, and the gallop, correspond to gaits adopted by distinct microalgal species. When the appendages are inserted perpendicularly around a central ‘body’, the robot achieved a net performance of 0.15–0.63 body lengths per cycle, with the trot gait being the fastest. Robotic swimming performance was found to be comparable to that of the algal microswimmers across all gaits. By creating a minimal robot that can successfully reproduce cilia-inspired drag-based swimming, our work paves the way for the design of next-generation devices that have the capacity to autonomously navigate aqueous environments.

1. Introduction

The capacity for self-generated movement is a distinguishing feature of most living organisms. In the macroscopic world, locomotion is typically associated with inertia [1], though recent work has revealed the dominance of friction in terrestrial movement [2, 3]. On the other hand, movement at the microscopic scale is subject to low Reynolds number physics, and cannot take advantage of inertial coasting. Without motility, a bacterium can only coast a minuscule distance an order of magnitude below the Ångström scale [4]. Over billions of years of evolution, microorganisms have become adept at
swimming, evolving distinct mechanisms for powering and maintaining self-propulsion through a fluid, often achieving speeds of several tens of cell-body lengths per second. This active motility confers a significant survival advantage, allowing microbes to navigate freely toward regions or locations where nutrients or resources are more plentiful [5]. Depending on the arrangement and number of locomotor appendages, single cells can execute swimming gaits that are surprisingly reminiscent of animals. For example, the model biflagellate alga *Chlamydomonas* actuates two equal-length flagella in a breaststroke [6], while quadriflagellate algae (single cells with four flagella) exhibit distinctive quadrupedal gaits such as the trot or the gallop [7] (figures 1(A) and (B)).

In recent years, advances have been made in understanding the biomechanics of microswimming. Here, the Reynolds number is small, $Re = UL/\nu$, where $L$ is a typical lengthscale of the swimmer, $U$ a typical velocity scale, and $\nu$ is the kinematic viscosity of the fluid. Equally important is the oscillatory Reynolds number $Re^{osc} = L^2\omega/\nu$ [8], where $\omega$ is the typical stroke frequency (which sets a tip velocity of $\omega L$). When both are small, flows are then governed by the Stokes equations: $0 = \nabla p - \mu \nabla^2 \mathbf{v}$ and $\nabla \cdot \mathbf{v} = 0$ (where $\mathbf{v}$ and $p$ are the flow and pressure fields), and have no explicit time-dependence. Microorganisms are able to break time-reversal symmetry using non-reciprocal strokes or body deformations, often involving whip-like appendages called cilia and flagella [4, 9]. While bacteria make use of rigid helical flagella [10], eukaryotes actuate motile cilia which produce asymmetric waves of propulsion [11, 12]. For a microorganism oscillating a 10 $\mu$m flagellum at 50 Hz, $Re \sim 10^{-3}$, and $Re^{osc} \sim 10^{-2}$. One further asymmetry is required for forward propulsion [13]: in living cells this can be achieved by shape asymmetry, which is ensured by the slender aspect ratio of all cilia and flagella (about 100). Rigid colloidal particles can also self-propel by diffusiophoresis without shape changes by generating concentration gradients [14]. A rod sweeping through a fluid in the direction perpendicular to the axis of the rod experiences approximately twice the drag compared to when it is moved in the parallel direction [15]. Organisms across all scales have been found to exploit this basic anisotropy for locomotion [3, 16, 17].

Despite the adoption of cilia and flagella as a common propulsion mechanism, the microscale locomotion strategies of microorganisms have diversified significantly across different phyla [18]. It is not well-understood why different gaits exist nor how they are coordinated. For centuries, locomotor gaits have been studied in the context of terrestrial animals, where the sequences of relative movement sustained by subsets of limbs or legs have fascinated researchers. In vertebrates, gaits are thought to be generated by central pattern generators [19]. But how can orderly, deterministic appendage coordination occur in single cells in the absence of nervous control [18, 20]? Recent theoretical and experimental work have shown that dynamic gait selection, at least in flagellates, appears to be an active and species-dependent process driven by intracellular and mechanical coupling [20, 21]. Notably, distinct quadriflagellates can self-propel at different speeds despite an apparently identical arrangement of flagella around the cell body [7, 22]. Since the ancestral form of the green algal lineage may have been a unicell with four flagella [23], there is much incentive to understand the precise mechanisms of appendage coordination in such systems.

In the quest to address these open questions of movement control, extant organisms can provide only a limited parameter space of possibilities in terms of size, shape, beat frequency, etc, often making it challenging to investigate certain configurations or physical regimes. Theoretical and computational approaches have been instrumental in shaping our understanding of active propulsion [15, 24], but these can be computationally expensive or reliant on simplifying assumptions. Meanwhile robophysical modelling has emerged as a powerful and versatile technique for elucidating organismal behavior by engineering customised configurations that can be easily tested in controlled laboratory settings [25–27]. The revolution in robophysical modelling has been driven in part by low cost electronics (motors, microcontrollers), and increasingly accessible control technologies that can complement theoretical modelling to provide real biological insights [26, 28]. However, trying to model cell movement is a significant conceptual challenge when working at the microscale. Even though increasingly controllable micro- and nanodevices have been fabricated to mimic the locomotive behaviors of biological swimmers [29, 30], these are overwhelmingly driven by external magnetic, electric or chemical fields. Magnetic fields are often unable to deliver the fine spatial control, required to independently actuate individual artificial cilia in a given array or network though there have been some recent progress in device miniaturisation [31]. As theoretical representations of flagellates, artificial swimmers and microrobots, minimal models based on a small number of moving components (beads, rods) have yielded significant insights into the effect of gait coordination on self-propulsion and motility [32–35]. Meanwhile, more realistic models of propulsive organelles that account for filament elasticity and shape have also been developed for single or arrays of cilia [36–38], but these approaches have not yet been applied to evaluate the influence of swimming gait in freely-moving multiflagellates.

The intrinsic limits of device manufacture at small scales severely undermines the suitability of microbots as realistic models of cell motility. To understand the influence of gait on self-propulsion
at low-Reynolds number, our goal is to build a dynamically-scaled robophysical model which is truly self-powered, where the movement of individual locomotor appendages can be prescribed and controlled independently. In contrast to traditional ‘microrobots’, the larger size allows us to explore and take advantage of increasingly sophisticated electronics and control architectures [39, 40]. We can readily reprogram these ‘roboflagellates’ to execute specific swimming gaits, making them well suited to testing theories of bio-inspired and autonomous locomotion at low-Reynolds number. This paper is organised as follows: We first identified and measured the relative swimming performance of three species of quadriflagellate algae that exhibit near-identical morphology but distinct swimming speeds. Next we built an O(10)cm robot that can self-propel in high-viscosity fluid when mimicking the asymmetric beat pattern of the algal flagella, verifying that low-Reynolds number kinematics are recapitulated. By arranging the robotic flagella in one of two possible configurations (parallel or perpendicular) relative to a central ‘cell body’, we imposed and tested three distinct flagellar actuation patterns (gaits) that occur naturally in the algal flagellates, namely the pronk, the trot, and the gallop. In each case, we compared the hydrodynamic swimming performance of the robot to that of the corresponding algal species. Finally, we discuss the relevance of these results for understanding how functional differences in swimming performance may arise from morphologically similar structures, and highlight the implications of this from an eco-evolutionary perspective.

2. Methods

2.1. Microalgal culturing and imaging

Three species of algae (Pyramimonas parkeae, Pyramimonas tetrarhynchus and Carteria crucifera) were cultured axenically according to previously published protocols [7, 20]. Free-swimming individuals were tracked in open microfluidic chambers using a high-speed camera (Phantom Vision Research). Brightfield imaging was conducted with 40× or 60× objectives using standard inverted microscopes (Leica DMi8 and Nikon T2000-U) under white light illumination. Free-swimming trajectories were obtained from high-speed videos in which single
cells crossed the focal plane, with the use of the open source software TrackMate (Fiji) [41]. Ten cells per species were used to determine the performance of each swimming gait (supplementary video 1 (https://stacks.iop.org/BB/16/066001/mmedia)). Tracks in which cells performed transient gaits, tumbles, or changed directions were not used in this analysis. The body length of each cell was measured along the long axis (anterior-posterior) of the organism. An average body length of 13.95 ± 2.05 μm, 12.54 ± 0.65 μm, and 12.82 ± 0.72 μm was found for *P. parkeae*, *P. tetrarhynchus* and *C. carteria* respectively.

### 2.2. A self-powered roboflagellate

We designed a dynamically-scaled robot to ensure that the robophysical model is self-powered and did not require external fields—all controllers and servos are fully self-contained (figure 1(C)). We performed robotic experiments in a highly viscous fluid (mineral oil, McMaster, 1000 cSt, product No. 1401K75) to approximate the center of geometry of the organism. Foam (FOA-3.5 kg/0.34 Nm, operating at 4.8 V). Each appendage (Savox, product No. SW0250MG, max torque of 3.7 kg/0.34 Nm, operating at 4.8 V). Each appendage was independently actuated by waterproof servo motors (Actuonix, product No. B07FQWDTTH7) of comparable viscosity to the mineral oil, to enable better visualisation and tracking of appendage movement. Each robot consisted of a 3D printed body (length and width = 8.5 cm, height = 2 cm) attached to four flagella that were independently actuated by waterproof servo motors (Savox, product No. SW0250MG, max torque of 3.5 kg/0.34 Nm, operating at 4.8 V). Each appendage was oriented such that the stroke lies in the plane perpendicular to the body (figure 1(C)). Foam (FOAMULAR Insulating Sheathing (IS) XPS Insulation) was attached on the robot body to achieve neutral buoyancy, allowing it to swim untethered. Commanded appendage positions were achieved using a micro-controller (Photon, Particle, part ID: PHOTONH) that allowed actuation of the robot with the use of Wi-Fi. The microcontroller and each motor were connected via an IOT Servo Shield (Actuonix, part ID: IOT-SHIELD-PHOTON), a circuit board specific to our micro controller. Four LEDs were placed on the 3D printed body to facilitate tracking. The robot was powered with three lithium ion polymer batteries (3.7 V, 2500 mAh), each powering directly the micro controller, the motors, and any attached LEDs. With this micro controller, the robots were able to sustain self-propulsion over approximately one hour.

### 2.3. Actuation of robotic flagella

Inspired by the flagellar beating waveform of the organisms, we implemented a simple two-link robotic flagellum connected via a 3D printed joint (figure 2). Each robotic appendage (length = 6.5 cm, diameter = 3.1 mm, polypropylene-based thermoplastic elastomer) could bend passively to break time-reversal symmetry, without the need to actively prescribe the shape of the flagella over a beat cycle (figure 2(B)). No external control such as magnetic fields were used; our robot was completely open loop. Each gait maintained a constant phase difference between adjacent flagella set by prescribed joint angles of the proximal segment (figure 3, supplementary video 2). Each gait was uploaded to the microcontroller via Wi-Fi, allowing the controllers to actuate the motors. Unless otherwise specified, all gaits were prescribed with a flagellar beat frequency of 0.14 Hz.

For the movement of the robot in mineral oil (kinematic viscosity $\mu/\rho = 10 \text{ cm}^2 \text{ s}^{-1}$), the Reynolds number for the body ($Re$) was 0.14 ($L = 3.8 \text{ cm}$, $U = 0.38 \text{ cm s}^{-1}$), while the oscillatory Reynolds number $Re_{osc}$ was 0.20 ($L = 3.8 \text{ cm}$, $\omega = 0.14 \text{ Hz}$). For the experiments conducted in glycerin (kinematic viscosity $\mu/\rho = 11.83 \text{ cm}^2 \text{ s}^{-1}$), $Re = 0.27$ ($L = 6.89 \text{ cm}$, $U = 0.40 \text{ cm s}^{-1}$), and $Re_{osc} = 0.55$ ($L = 6.89 \text{ cm}$, $\omega = 0.14 \text{ Hz}$).

### 2.4. Prescribing the swimming gait in the roboflagellate

We imposed three distinct gaits on the robot similar to those observed in quadriflagellate algae—the pronk, the trot, and the gallop. The different coordination patterns were achieved by prescribing the phase differences between adjacent appendages. The resulting gait sequences were confirmed for an immobilised robot body, where the distance from each flagellum tip to the cell body was used as proxy for phase. In the pronk gait, all four appendages move simultaneously, without any phase difference ($\varphi = 0^{\circ}$) between adjacent flagella (figure 3(A)). The trot gait is defined by alternating pairs of flagella each of which is generating a pattern analogous to a breaststroke, with a phase difference of half a gait cycle ($\varphi = 180^{\circ}$) (figure 3(B)). In the gallop gait, each appendage moves with a phase difference of a quarter-gait cycle relative to its neighbor (figure 3(C)). The directionality (clockwise (CW) or counter-clockwise (CCW)) of the gallop gait is determined by the phase difference ($\varphi$) between the first appendage ($m_1$) and an adjacent appendage ($m_2$ or $m_3$). We tested the gallop gait in both a CW ($\varphi = 90^{\circ}$ between $m_1$ and $m_2$) and CCW ($\varphi = 180^{\circ}$ between $m_1$ and $m_2$) direction. We imposed either a CW and CCW direction to investigate how chirality can affect the performance of the gallop gait.

### 2.5. Motion tracking

Due to the opacity of the oil, we attached lightweight LEDs to the robot’s body to enable motion tracking. All LEDs were digitized using custom MATLAB algorithms. We approximated the center of geometry of the robot by averaging the position of the LEDs over time. Then, we used the tracks to determine the distance traversed by the robot in units of body lengths.
per beat cycle. A total of 9 trials were taken per gait, for each robot configuration. A trial was terminated either when the robot contacted a boundary, or if the LEDs were no longer visible as the robot slowly drifted downwards over time; this is due to the 3D material trapping fluid and increasing in mass. Each trial comprised 6–10 beat cycles per gait. In subsequent experiments, we used glycerin as an alternative high viscosity fluid to visualize and track movement of the flagella during active swimming. However, because glycerin is not a dielectric fluid, Wi-Fi connectivity was interrupted and the circuits were negatively affected. To resolve this, we substituted our microcontroller (Pro Trinket, Adafruit, product ID: 2000) and sealed the circuits with a gasket and a 3D printed cap. In glycerin, flagella kinematics were digitized using DLTdv8 [43].

3. Results and discussion

3.1. The trot is the fastest gait in the algae

We identified the quadriflagellates as an ideal study group owing to their morphological diversity (in size, shape, aspect-ratio), and abundance in marine, terrestrial as well as freshwater habitats. A key trait among quadriflagellate genera is the arrangement or insertion of flagella around the anterior of the cell [23, 44]. Here we take advantage of this diversity to compare the swimming behavior of three species (P. tetrarhynchus, P. parkeae, and C. crucifera) that employ three distinct gaits—respectively the pronk, the trot, and the gallop (supplementary video 1). We conjecture that inter-species differences in quadriflagellate swimming performance can be attributed to differences in gait alone—where the same basic stroke is applied to ensembles of appendages but according to distinct phase relationships.

Figure 2. Breaking time-reversal symmetry with a hinged, two-link, bio-inspired flagellum. One beat cycle of an (A) algal flagellum compared to a (B) robot flagellum. P: power stroke (red), R: recovery stroke (blue). Each robot flagellum segment has a length of 6.5 cm and diameter of 3.1 mm. Asymmetric beat patterns are achieved via a 3D printed joint. The movement patterns of the algal flagellum were measured in water. Robot beat patterns were visualized in a high-viscosity fluid (glycerin).

Two of these algae belong to the genus *Pyramimonas*, a Prasinophyte algae belonging to an early diverging class which is thought to have given rise to the core chlorophyte algae, comprising species with two, four, eight, or up to sixteen flagella [7, 45]. Four flagella of identical length and beat pattern emerge from an deep anterior groove or pit in the cell body. The third species, *C. crucifera*, is a Volvocalean flagellate that is closely related to the model biflagellate *Chlamydomonas*. Despite this phylogenetic divergence, all three species are similar in body size and flagellar morphology, and appear obovoid (egg-shaped) to cordate (heart-shaped) in side profile [46, 47].

In all three cases, cells swim smoothly flagella-first (puller-type) at speeds of $O(100) \mu m s^{-1}$. The translational motion is coupled to an axial rotation to produce swimming along helical trajectories [48]. Abrupt gait transitions can occur either spontaneously or when triggered by mechanical contact, during which the flagella are directed to the front of the cell in a so-called shock-response [49]. Cells can also reversibly stop and start swimming, when all or some of the flagella transiently cease to beat [20].

In all cases, free-swimming trajectories are super-helical, where small-scale swirls at the cell-scale are produced by the periodic flagellar oscillations. Three representative tracks, projected onto the focal plane, are shown in figures 4(A), (C) and (E). Using these tracks, we estimated for each of the three gaits the displacement per cycle, including the cumulative displacement as a function of phase during the beat cycle (figure 4(G)) as well as the mean forward progress per complete cycle (figure 4(H)). Measured swimming speeds were $126 \pm 24 \mu m s^{-1}$ for the pronk, $408 \pm 46 \mu m s^{-1}$ for the trot, and $127 \pm 25 \mu m s^{-1}$ for the gallop. Our results show that...
the trot gait is the fastest gait in the microalgae. Meanwhile the pronk and gallop gaits lead to comparable propulsion speeds.

3.2. A hinged flagellum breaks time-reversal symmetry

We first confirmed that our robophysical model resides in a low-Reynolds number regime by attaching 3D-printed rigid (unhinged, length = 13 cm) flagella to the body, and actuating these with both a time-symmetric as well as a time-asymmetric stroke pattern. To create a time-asymmetric stroke, we increased the beating frequency of the recovery stroke. Due to the rotational position based control of the motors, changes in the frequency were achieved by changing the rate at which joint angles were prescribed. The recovery stroke frequency was varied from 0.07 Hz to 0.21 Hz (supplementary video 3). As expected, reciprocal strokes produced negligible net swimming in both cases. For a time-symmetric pattern, the net displacement in the direction of movement after one complete cycle was $0.38 \pm 0.40$ cm ($0.05 \pm 0.05$ BL) using the pronk gait (figure 5(A)). When the stroke frequency was increased, and consequently Reynolds number, the displacement of the robot increased (figure 5(B)). Thus, at higher beat frequencies the system can reach intermediate Reynolds numbers. Hereafter, we use a flagella beat frequency of 0.14 Hz to ensure inertial effects remain negligible.

With hinged instead of rigid flagella (figure 2(B)), the robot became capable of net forward propulsion. Each gait cycle can be characterized by a power stroke during which the robot gains distance, and a recovery stroke during which it loses distance. We first set out to test the effect of flagella ‘waveform’ on swimming performance, this is expected to scale approximately with stroke amplitude [50, 51].
Figure 4. Gaits, kinematics, and hydrodynamic performance of quadriflagellate algae. All experiments were conducted in culture media—which had the same viscosity as water. For the pronking gait of *P. tetrahyrncus*: (A) a sample (cell-centroid) trajectory coloured by time, and (B) forward displacement over time for three cycles. Inset shows forward displacement over time of trajectory. For the trotting gait of *P. parkeae*: (C) a sample (cell-centroid) trajectory coloured by time, and (D) forward displacement over time for three cycles. Inset shows forward displacement over time of trajectory. For the galloping gait of *C. crucifera*: (E) a sample (cell-centroid) trajectory coloured by time, and (F) forward displacement over time for three cycles. Inset shows forward displacement over time of trajectory. (G) Mean displacement within a gait cycle for all gaits—the pronk (blue line), trot (red line), and gallop (black line). Shaded areas correspond to the standard deviation. (H) Median displacement computed in terms of body lengths per cycle, for each gait. Red crosses correspond to outliers. Asterisks correspond to statistical significance of differences observed. Differences are significant at $p \leq 0.01$, $p \leq 0.001$ for two and three asterisks, respectively.

3.3. Flagellar undulation pattern affects swimming performance

We implemented two distinct flagellar undulation patterns—as defined by the maximal sweep range of the segments. For simplicity and to prevent axial rotation, we reduced our quadriflagellate robot to a biflagellate robot, by removing one pair of flagella (supplementary video 4). The remaining pair of flagella was programmed to follow a breaststroke pattern (figure 6(A)). We prescribed and compared the swimming performance for two different sets of motor angles for the proximal segment: (i) $[0^\circ, 180^\circ]$, and (ii) $[45^\circ, 135^\circ]$ (figure 6(A) inset). The motion of the distal segment always follows passively, with the hinge breaking time-reversal symmetry. We tracked the flagella ‘waveform’ in the two cases and calculated the angles generated by each flagellum segment over time (from motor to joint and from joint to tip, figure 6(A)). The two sweep amplitudes produced two distinct gaits in the $\theta_1-\theta_2$ shape space figure 6(B).

A reduced sweep range results in a higher beat frequency ($\omega = 0.14$ Hz for motor angles of $[0^\circ, 180^\circ]$), and $\omega = 0.41$ Hz for motor angles of $[45^\circ, 135^\circ]$). The rescaled displacement shows swimming performance increases with stroke amplitude (figure 6(C)). The larger-amplitude breaststroke achieves a greater displacement after each gait cycle. This suggests that non-inertial locomotion is dictated by geometric mechanics, as shown previously in the case of infinitesimal deformations [50]. Here, movement is kinematic, and net displacement is determined largely by the gait and its associated low-dimensional properties [52].

3.4. Roboflagellate swimming performance depends on gait and appendage placement

To test if swimming performance is dominated by gait or by other factors such as flagellar stiffness or waveform compliance, we prescribed the gaits exhibited by each algae species to our roboflagellates. We explored the effect of varying appendage phase coordination
Figure 5. Kinematic reversibility confirms low-Reynolds regime. (A) Forward displacement travelled over time in glycerin with either a time-symmetric and time-asymmetric stroke pattern. Frequency of power and recovery stroke was 0.07 Hz for the time-symmetric stroke pattern. Frequency of the power and recovery stroke was 0.07 and 0.12 Hz, respectively for the time-asymmetric pattern. The robot achieved negligible net displacement per cycle with either stroke pattern. Inset shows one beat cycle of a single rigid flagellum moving back and forth. P: power stroke, R: recovery stroke. (B) Mean displacement as a function of stroke frequency. Star corresponds to frequency used for experiments shown for the rest of the experiments, unless otherwise stated. Error bars correspond to standard deviation. Snapshots of the robot during one gait cycle using rigid flagella for time-symmetric (C) and time-asymmetric (D) stroke pattern. Left panel (outlined in red) shows the robot initiating a power stroke. Middle panel shows the robot during half a cycle. Right panel (outlined in blue) shows the end of the recovery stroke. Dashed lines highlight initial positions.

(gait) for two different configurations of four flagella, in which motors are positioned either in a parallel or a perpendicular orientation with respect to an identical body.

These configurations were modeled on naturally-occurring arrangements of basal bodies and flagella found in extant algal flagellates (figure 7). All three species of algae studied here correspond to configuration A, in which the approximate plane of flagellar beating is perpendicular to the surface of the robot body. The main difference is that when viewed from the anterior of the cell, the four flagella are inserted with a clockwise twist or offset for *Carteria*, but an anticlockwise offset for *Pyramimonas* [44]. Algal species reported to exhibit configuration B [44] were not available in culture and were not represented in the present study. Appendage coordination was prescribed in the robot by specifying the phase differences between flagella, to produce each of the three gaits: pronk, trot, or gallop, as previously described (figure 3).

For the perpendicular configuration, example trajectories as well as the cumulative forward displacement over time for each gait are shown in figures 8(B), (C) and (E)–(J)). We also analyzed the detailed within-cycle dynamics for each gait (supplementary video 5). The pronk and both the CW gallop and CCW gaits produce significant forward displacement during the power stroke (up to 5.7 cm for the pronk, 4 cm and 2 cm for the CW and CCW gallops respectively after half a gait cycle), but also produce a significant backward displacement during the recovery stroke, generating overall small displacement from cycle to cycle (0.33 ± 0.04 BL/cyc, 0.16 ± 0.05 BL/cyc, and 0.15 ± 0.08 BL/cyc for the pronk, the CW gallop, and CCW gallop respectively). On the other hand, while the trot does not achieve a greater displacement (only 2.3 cm after half a gait cycle) than the pronk.
or gallop during the power stroke, it loses a much smaller distance during the recovery stroke. This is because while one pair of flagella is moving toward the body and consequently producing backward motion, the other pair of flagella moves away from the body so as to resist this motion. This can also be observed in the trajectories, where the pronk and gallop gaits show backward motion, unlike the trot gait. Due to this, of the three gaits investigated the robot achieves the greatest hydrodynamic performance (0.6 ± 0.08 BL/cyc) using the trot gait (figure 8(K)), just as in the algae.

For the parallel configuration (supplementary video 6), example trajectories as well as the forward displacement over time for each gait can be seen in figures 9(B), (C) and (E)–(J). Similar to the perpendicular configuration, the pronk gait allows the robot to gain a significant amount of distance during the power stroke (up to 5 cm after half a gait cycle) but also lose a significant amount of distance during the recovery stroke, generating little net displacement from cycle to cycle. The gallop gait in the CCW displays a similar oscillatory pattern, however there is a discrepancy between the CCW and CW gallops (5.3 cm after half a gait cycle for the CW gallop, but only 1 cm for the CCW gallop). This is likely due to rotation-translation coupling in the second configuration (in which the flagella are inserted in the CCW sense), generating significant motion laterally and causing axial rotation of the robot. Similar to the perpendicular robot, the trot gait advances less during

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**Figure 6.** Swimming performance increases with stroke amplitude. (A) Quadriflagellate robot modified as a biflagellate robot, performing a breaststroke pattern with one pair of flagella. Angles $\theta_1$ and $\theta_2$ correspond to the angles generated by the flagella segment from the motor (white circle) to the joint (dark orange circle) and the segment from the joint (dark orange circle) to the tip (light orange circle). Inset shows variation of prescribed angles from $0^\circ$ to $180^\circ$ (green) and from $45^\circ$ to $135^\circ$ (blue). (B) $\theta_1$ as a function of $\theta_2$, coloured by time. Green dots corresponds to angles from $0^\circ$ to $180^\circ$. Blue dots corresponds to $45^\circ$ to $135^\circ$. (C) Displacement travelled over time. Green line corresponds to angles from $0^\circ$ to $180^\circ$. Blue line corresponds to $45^\circ$ to $135^\circ$. (D) Mean displacement as a function of a gait cycle. Green line corresponds to angles from $0^\circ$ to $180^\circ$. Blue line corresponds to $45^\circ$ to $135^\circ$. Shaded areas correspond to the standard deviation. These experiments were conducted in glycerin with the alternative robot, to ensure the flagella beat pattern can be tracked.

**Figure 7.** Modelling appendage orientation. (A) Illustration of two configurations of flagella and basal bodies that are found in quadriflagellates [44]. The flagella emerge from basal bodies (cylinders) that are oriented largely perpendicular (A), or parallel (B) to the cell body. Insets show anterior views (A: cruciate arrangement, B: turbine or windmill-like). Double-arrow indicates the approximate beat plane of the individual flagella. Similarly, two roboflagellate designs are presented. Motors and attached ‘flagella’ are oriented perpendicular (C) or parallel (D) to the central body. Again, double-arrow indicates oscillation plane.
Figure 8. Swimming gait kinematics and performance for robot with flagella in the perpendicular orientation. (A) Diagram of robot with motors oriented perpendicular to the body. Inset illustrates beating plane. For the pronk gait, (B) shows a sample trajectory of the robot, coloured by time (5 cycles), and (C) the forward displacement travelled over time. For one gait cycle, red vertical lines highlight power stroke, and blue vertical lines highlight return stroke. (D) Snapshots of the robot during one cycle of the pronk gait. Left panel (outlined in red) shows the robot initiating a power stroke. Middle panel shows the robot during half a cycle. Right panel (outlined in blue) shows the robot completing the recovery stroke. (Arrow: swimming direction.) Trajectory of the robot during the trot gait, coloured by time (5 cycles) (E), and forward displacement travelled over time of the robot during the trot gait (F). Trajectory of the robot during the CW gallop gait, coloured by time (5 cycles) (G), and forward displacement travelled over time of the robot during the CW gallop gait (H). Trajectory of the robot during the CCW gallop gait, coloured by time (5 cycles) (I), and forward displacement travelled over time of the robot during the CCW gallop gait (J). (K) Mean displacement over a gait cycle for all gaits—the pronk (blue line), trot (red line), CW gallop (black line), and CCW gallop (gray line). Shaded areas correspond to the standard deviation. (L) Body length per cycle as a function of swimming gait. Red crosses correspond to outliers. Asterisks correspond to statistical significance of differences observed. Differences are significant at \( p \leq 0.001 \) for three asterisks.
Figure 9. Swimming gait kinematics and performance for robot with flagella in the parallel orientation. (A) Diagram of robot with motors oriented perpendicular to the body. Inset illustrates beating plane. For the pronk gait, (B) shows a sample trajectory of the robot, coloured by time (5 cycles), and (C) the forward displacement travelled over time. For one gait cycle, red vertical lines highlight power stroke, and blue vertical lines highlight return stroke. (D) Snapshots of the robot during one cycle of the pronk gait. Left panel (outlined in red) shows the robot initiating a power stroke. Middle panel shows the robot during half a cycle. Right panel (outlined in blue) shows the robot completing the recovery stroke. (Arrow: swimming direction.) Trajectory of the robot during the trot gait, coloured by time (5 cycles) (E), and forward displacement travelled over time of the robot during the trot gait (F). Trajectory of the robot during the CW gallop gait, coloured by time (5 cycles) (G), and forward displacement travelled over time of the robot during the CW gallop gait (H). Trajectory of the robot during the CCW gallop gait, coloured by time (5 cycles) (I), and forward displacement travelled over time of the robot during the CCW gallop gait (J). (K) Mean displacement over a gait cycle for all gaits—the pronk (blue line), trot (red line), CW gallop (black line), and CCW gallop (gray line). Shaded areas correspond to the standard deviation. (L) Body length per cycle as a function of swimming gait. Red crosses correspond to outliers. Asterisks correspond to statistical significance of differences observed. Differences are significant at $p \leq 0.001$ for three asterisks.
the power stroke (only 1.5 cm after half a gait cycle) and loses more distance during the recovery stroke, relative to the perpendicular configuration. The phasing between appendages in the trot gait again aids the robot in traversing a greater distance from cycle to cycle than the pronk (0.15 ± 0.4 BL/cyc), and also greater than the average of the CW and CCW gallop gaits (0.15 ± 0.9 BL/cyc). (We assume that by symmetry, this average between the two chiralities should cancel any rotational effects.) Thus, the trot remains a hydrodynamically effective gait for the parallel robot (0.26 ± 0.08 BL/cyc) (figure 9(K)).

We conclude that the swimming performance of the robofilagellate is highly sensitive to both gait and flagellar orientation (which defines the principal beat plane) of the flagella. It is possible that the organisms can access different regimes by controlling the 3D beat plane of their flagella, and that divergent flagellar placement evolved in different species as a result of different environmental selection pressures. In multicellular flagellates such as Volvox, nearby basal bodies (from which the flagella emerge) have rotated 90 degrees compared to the ancestral configuration found in the unicellular Chlamydomonas, likely to facilitate coordinated flagellar beating as an intact colony [7, 53].

3.5. Speed of robofilagellate is comparable to that of algae

The above results show that a change in flagellar configuration can significantly change the performance of a given swimming gait. Focusing only on the trot, we note that this gait yielded the highest hydrodynamic performance for the algae and for the perpendicular robot, (figure 10). Note that the speed of the algae trot gait is bounded above and below by that of the perpendicular and parallel robots.

In both robot configurations, significant axial rotation and lateral movement were observed in the free-swimming trajectories (figures 10(E) and (H)) showing that our robophysical models do not swim as smoothly as their algal counterparts (figure 10(B)). This is likely due to the discrepancy between the deformable stroke cycle of the continuous algal flagellum, compared to the angular movements of the two-link robot flagella. Additionally elastic elements in the algal cytoskeleton could play a role in gait stabilization by actively anchoring the flagella to the body [21, 54]. The cumulative displacement over time for a trotting cell and our perpendicular robot are comparable (figures 10(C) and (F)). Meanwhile the parallel configuration displays larger amplitude oscillations in which a greater distance gained during each power stroke is negated during the subsequent recovery stroke (figure 10(I)). This is likely due to three-dimensional effects as mentioned above. In all, we find that the performance of the algae and both robofilagellate configurations are comparable in absolute terms, as measured in terms of body lengths per stroke cycle. This agreement is surprising as we did not precisely match the dimensions of our robots to that of the algal cell, and unlike the algal flagella the robot ‘flagella’ were not capable of active bending [9]—being comprised only of rigid tubing and a plastic hinge.

4. Conclusion and future work

Microscopic organisms have evolved to harness many different ways of swimming at low-Reynolds number. Despite their size and simplicity, some single-celled algae can swim with different speeds using gaits analogous to animal gaits, that involve robust temporal ordering of four flagella [20]. Here, we created the very first free-swimming robophysical model of these microswimmers to understand how motility and gait influences swimming. Dynamically-scaled robots enable scenarios to be tested that may...
not be possible in the live organism [55–58]. Physical modelling has previously provided insights into bacterial swimming [59], flagellar bundling [60], elastic tail propulsion [61], and metachronal actuation of in an on-rail robot with rigid appendages [62].

In contrast, our roboflagellate is self-powered and untethered (no external forces or torques) and was able to achieve fully-3D self-propulsion at low-Reynolds number. The robot recapitulated gait-dependent differences in swimming performance that we measured in the microalgae. These results reveal that phase coordination of propulsive appendages has a significant impact on hydrodynamic performance, while the orientation of appendages relative to the swimmer body also changes propulsion speed. In the perpendicular configuration that most closely models the three algal species studied here, the trot gait was consistently faster than either the pronk or gallop gait. We further predict that quadriflagellates with flagella oriented parallel to the cell body (configuration B) should swim more slowly than the three species studied here, for an equivalent gait. Moreover in all cases the displacement achieved by the robot in terms of body lengths per cycle was similar in absolute terms to the algae. Thus our dynamically-scaled robot is a good locomotor model of the biological microswimmer.

Our work raises open eco-evolutionary questions about the origins of the distinct motility patterns in the different quadriflagellate species. Distinct gaits likely reflect a more nuanced relationship between an organism’s metabolic requirements and its habitat. Freely-locomoting organisms at all scales, switch dynamically between multiple gaits [5, 63, 64]. While several *Pyramimonas* species exhibit sporadic bursts of rapid activity with extended quiescent phases [49], *Volvocalean* algae including *Carteria* do not show such rest periods [20]. We conjecture that differences in gait confer an evolutionary advantage even at the microscale. Of the three algae studied here, two (*P. tetrarhynchus*, *C. carteria*) are freshwater species and one is a marine species (*P. parkeae*). *P. tetrarhynchus* (type species) was originally isolated from a peaty pool and cultured in a biphasic soil medium [46]. *C. crucifera* is also a freshwater species that forms surface associations with leaves and other decaying material. In contrast *P. parkeae* is most abundant in Arctic surface water and in tidal rock pools, where it can access sufficient sunlight for photosynthesis. *P. parkeae* also exhibits a unique diurnal vertical settling behavior [65]. The latter behavior, along with phototaxis, accentuates the requirement for vigorous swimming and hence the fast trot gait. Field data has shown that marine *Pyramimonas* routinely blooms in and around sea ice, where the unique polar environment (extreme fluctuations in temperature, light, salinity etc) is associated with a highly heterogeneous distribution of different *Pyramimonas* species even within the same water column [66]. The habitats of these algae may therefore be a key evolutionary driver leading to significant diversification of gait, even across species with apparently convergent morphology and size [67, 68]. Further experiments using both lab strains and wild isolates, controlling more precisely for culturing medium, are need to test this hypothesis. Our roboflagellate model can be used to explore mix-mode propulsion strategies and unsteady effects, such as nutrient dispersal.

We highlight two limitations of the current model. The first concerns boundary and finite-size effects, particularly due to fluid-structure interactions between moving appendages and the bounding tank, and between different parts of the robot. The presence of no-slip boundaries will alter the flow fields around a beating appendage, and change propulsion efficiency [69]. The chiral insertion of the robot flagella around the central body likely introduced an additional (unwanted) rotational movement. Second, the current robot relies on a two-link flagellum facilitated by a rigid 3D printed joint which has fewer degrees of freedom than the organisms. The rigid joints have limited ability to resist torsion—which may be gait-dependent. Eukaryotic flagella and cilia can maintain their shape even when subject to significant hydrodynamic forces. They can also deform actively, to optimise propulsive force generation and efficacy [70, 71]. In future work we can resolve these limitations with more realistic roboflagellate designs, in parallel with hydrodynamic simulations and modelling to understand gait optimisation with truly deformable appendages.

In conclusion, we have presented a macroscopic robot capable of self-propulsion at low-Reynolds number, and used this successfully to model aspects of microorganism swimming behavior. This approach has transformative potential for understanding different mechanisms of microscale swimming, e.g. gait selection, coordination and taxis [18]. These insights could have profound implications for how morphological computation may be achieved in aneural or early nervous systems. From a technological perspective, these diverse propulsion strategies can provide unique, innovative solutions to the formidable challenge of navigating viscous fluids.

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Data availability statement

All data that support the findings of this study are included within the article (and any supplementary files).

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